

Inference at \*  
of proof for Lemma can-apply-p-lift:

$\vdash \forall A, B:\text{Type}, P:(A \rightarrow \mathbb{P}), d:(x:A \rightarrow \text{Dec}(P(x))), f:(\{x:A \mid P(x)\} \rightarrow B), x:A.$   
 $(\uparrow \text{can-apply(p-lift}(d;f);x)) \iff P(x)$   
by (RepUR “can-apply p-lift“ ( 0)·)  
CollapseTHEN ((UnivCD)  
CollapseTHENA (Auto·)·)

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1.  $A : \text{Type}$
  2.  $B : \text{Type}$
  3.  $P : A \rightarrow \mathbb{P}$
  4.  $d : x:A \rightarrow \text{Dec}(P(x))$
  5.  $f : \{x:A \mid P(x)\} \rightarrow B$
  6.  $x : A$
- $\vdash (\uparrow \text{isl}(\text{case } d(x) \text{ of inl}(a) \Rightarrow \text{inl } (f(x)) \mid \text{inr}(a) \Rightarrow \text{inr } a)) \iff P(x)$